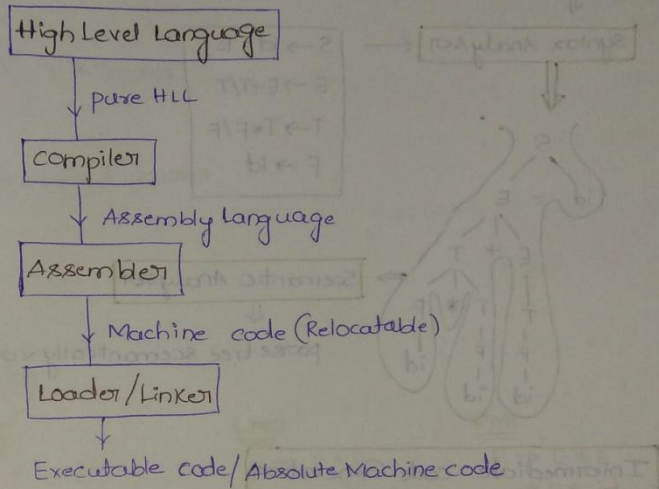


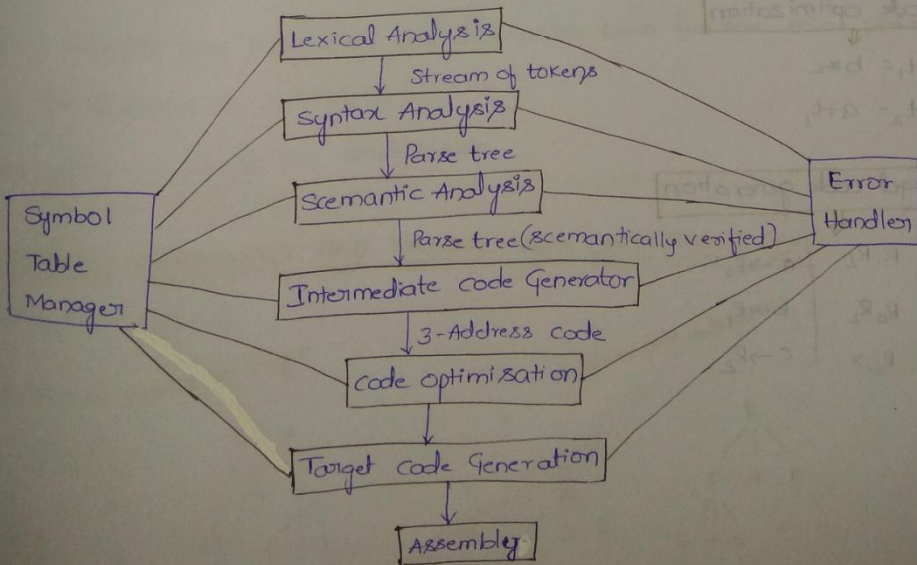
INTRODUCTION AND VARIOUS PHASES OF COMPILER (L-1)

⇒ The main aim of the compiler is to convert a High Level Language to Low level language.



⇒ Removing `#include` by including a specific file is called "File Inclusion".

⇒ "Assembler" is dependent on the platform [Hardware + OS].

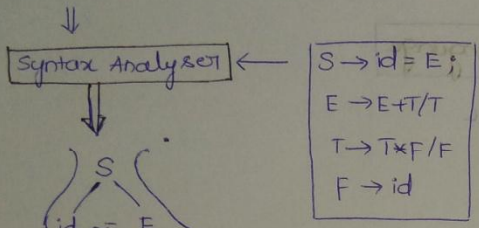


INTRODUCTION AND VARIOUS PHASES OF COMPILER

1)  $x = a + b * c$

↓  
**Lexical Analysis** ⇒ The Lexical Analyzer identifies the "identifiers," "tokens" using some Regular expressions called patterns  $1(id)^*$

$id = id + id * id$



**Semantic Analyzer**  
↓  
parse tree semantically verified

**Intermediate code Generation**

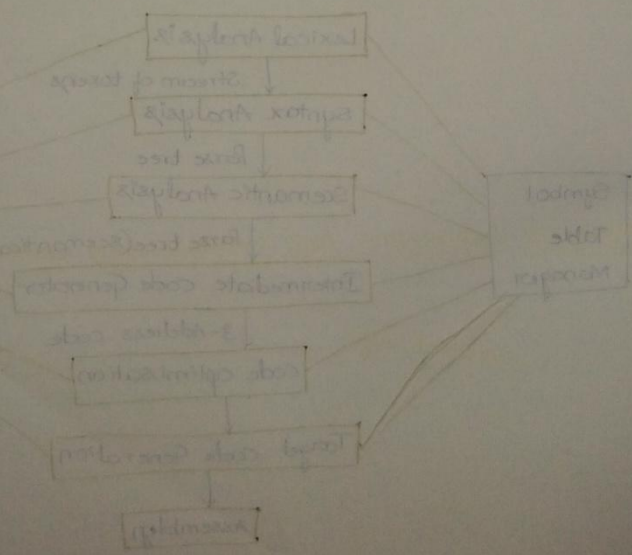
↓  
 $t_1 = b * c$   
 $t_2 = a + t_1$   
 $x = t_2$

**Code optimization**

↓  
 $t_1 = b * c$   
 $t_2 = a + t_1$

**Target code generation**

↓  
Mul  $R_1, R_2$  |  $a \rightarrow R_0$   
Add  $R_0, R_2$  |  $b \rightarrow R_1$   
Mov  $R_2, X$  |  $c \rightarrow R_2$



# INTRODUCTION TO LEXICAL ANALYSER (L-2)

⇒ This is the only phase that reads the Input character by character

⇒ int max(x,y)

int x,y;

/\* find max of x and y \*/

{  
  return (x>y?x:y);  
}

25 Tokens are present

int = 1 token

max = 1 token

return = 1 token

⇒ printf("%d Hai %d", x, y); ⇒ 8 Tokens  
1 2 3 4 5 6 7 8

⇒ Syntax Analyser is also called parser

## Grammar:

$E \rightarrow E+E / E * E / id$

⇒ id+id\*id = Given string

### LMD

$E \rightarrow E+E$

→ id + E \* E

→ id + id \* E

→ id + id \* id

### RMD

$E \rightarrow E+E$

→ E + E \* E

→ E + E \* id

→ E + id \* id

→ id + id \* id

### LMD

$E \rightarrow E * E$

→ E + E \* E

→ id + E \* E

→ id + id \* E

→ id + id \* id

### RMD

$E \rightarrow E * E$

→ E \* id

→ E + E \* id

→ E + id \* id

→ id + id \* id

⇒ If a Grammar has more than one derivation trees for the same string then the Grammar is Ambiguous

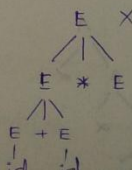
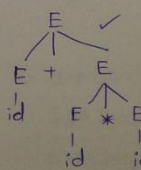
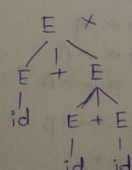
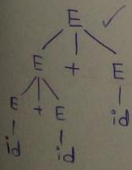
⇒ Ambiguity problems are undecidable

## AMBIGUOUS GRAMMARS AND MAKING THEM UNAMBIGUOUS (L-3)

$E \rightarrow E+E / E * E / id$

id+id+id ⇒ Associativity X

id+id\*id ⇒ precedence (X)



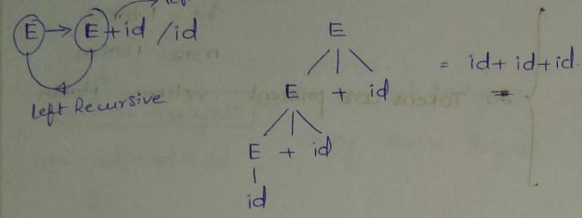
Leftmost plus should be evaluated first

Highest precedence one should be evaluated first (\* should be evaluated first)

REDUCTION TO LEXICAL ANALYSER (L-3)

To avoid the above Ambiguity we have to restrict the growth of the

Grammar.



⇒ The Grammar is said to be left recursive if the leftmost symbol in the RHS = LHS

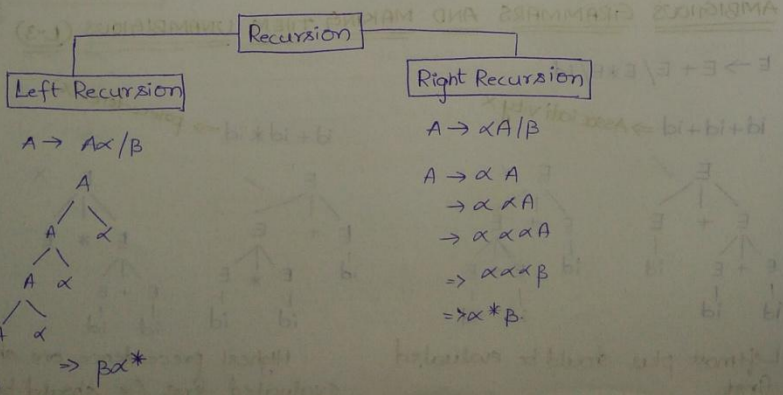
⇒ In order to overcome the Associativity we need to define the Grammar to be left Recursive

- ⇒  $E \rightarrow E + T / T$
  - ⇒  $T \rightarrow T * F / F$
  - ⇒  $F \rightarrow id$
- Associativity = Recursion  
Precedence = Levels

⇒  $2 * 3 * 1 * 2 = 2^{3^2} = (2)^{3^2} = 2^9$

- ⇒  $A \rightarrow A \$ B / B$
  - ⇒  $B \rightarrow B \# C / C$
  - ⇒  $C \rightarrow C @ D / D$
  - ⇒  $D \rightarrow d$
- $\$, \#, @ =$  Left Associative  
 $\$ \succ \$, \# \succ \#, @ \succ @$   
 $\$ \prec \# \prec @$

LEFT RECURSION ELIMINATION AND LEFT FACTORING OF GRAMMARS (L-4)



⇒  $P \alpha^* (A \rightarrow \dots)$

$A \rightarrow \beta A'$   
 $A' \rightarrow \alpha A' / \epsilon$

1)  $E \rightarrow E + T / T$   
 $A \rightarrow \alpha / \beta$

2)  $A \rightarrow \beta_1 A' / \beta_2$   
 $A' \rightarrow \alpha_1 A' / \alpha_2$

3) Grammars

G

Ambiguous

Left Recursive

Deterministic

1)  $S \rightarrow i E$   
 $E \rightarrow b$

⇒ The el

of Ar

2)  $S \rightarrow \alpha S$

3)  $S \rightarrow \beta S$

$$\Rightarrow \beta\alpha^*(A \rightarrow \beta\alpha^*)$$

$$\begin{cases} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' / \epsilon \end{cases} \iff \begin{cases} A \rightarrow \alpha A' / \beta \end{cases}$$

**PARSERS**

If the grammar is of the form  $A \rightarrow \alpha A / \beta$  then eliminate left recursion by  $\begin{cases} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' / \epsilon \end{cases}$

$$1) \begin{cases} E \rightarrow E + T / T \\ A \rightarrow \alpha A' / \beta \end{cases}$$

$$\begin{cases} E \rightarrow TE' \\ E' \rightarrow \epsilon / +TE' \end{cases}$$

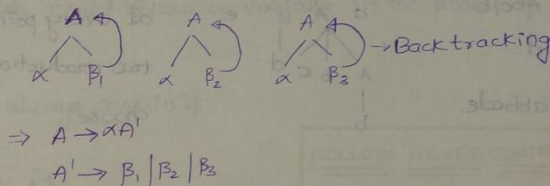
= Left Recursion Eliminated

$$2) \begin{cases} A \rightarrow B_1 A' / B_2 A' / B_3 A' \\ A' \rightarrow \alpha_1 A' / \alpha_2 A' / \alpha_3 A' \end{cases} \text{ is the eliminated LR of the Grammar } A \rightarrow \alpha_1 | \alpha_2 | \alpha_3 / \dots / \beta_1 / \beta_2 / \beta_3 \dots$$

3) Grammars can be classified into various categories

$G_1$

Ambiguous	unambiguous
Left Recursive	Right Recursive
Deterministic	Non-deterministic ( $A \rightarrow \alpha\beta_1 / \alpha\beta_2 / \alpha\beta_3$ )



$$1) \begin{cases} S \rightarrow iETs / iETsEs/a \\ E \rightarrow b \end{cases} \quad \begin{cases} S \rightarrow iETs/a \\ S' \rightarrow eS/e \\ E \rightarrow b \end{cases}$$

⇒ The elimination of Non-determinism doesn't guarantee the elimination of Ambiguity.

$$2) \begin{cases} S \rightarrow \alpha s s b s / \alpha s a s b / \alpha b b / b \\ S' \rightarrow \alpha s s b s / \alpha s a s b / \alpha b b \end{cases} \Rightarrow \begin{cases} S \rightarrow \alpha s' / b \\ S' \rightarrow s s' / s a s b / b b \\ S' \rightarrow s s'' \\ S'' \rightarrow s b s / a s b \end{cases}$$

$$3) \begin{cases} S \rightarrow b s s a a s / b s s a s b / b s b / a \\ S' \rightarrow s a s / s a s b / b \\ S \rightarrow S a s'' / b \\ S'' \rightarrow a s / s b' \end{cases}$$

# PARSERS

⑥

⇒ parsers are nothing but Syntax Analyzers. (L-5)

Now, Before functions

FIRST():

$S \rightarrow a ABC$

$A \rightarrow b$

$B \rightarrow c$

$C \rightarrow d$

$D \rightarrow e$

$S \rightarrow ABCD$

$A \rightarrow b$

$B \rightarrow c$

$C \rightarrow d$

$D \rightarrow e$

FOLLOW():

⇒ what is

derivati

⇒ follow o

$S \rightarrow ABCD$

$A \rightarrow b/e$

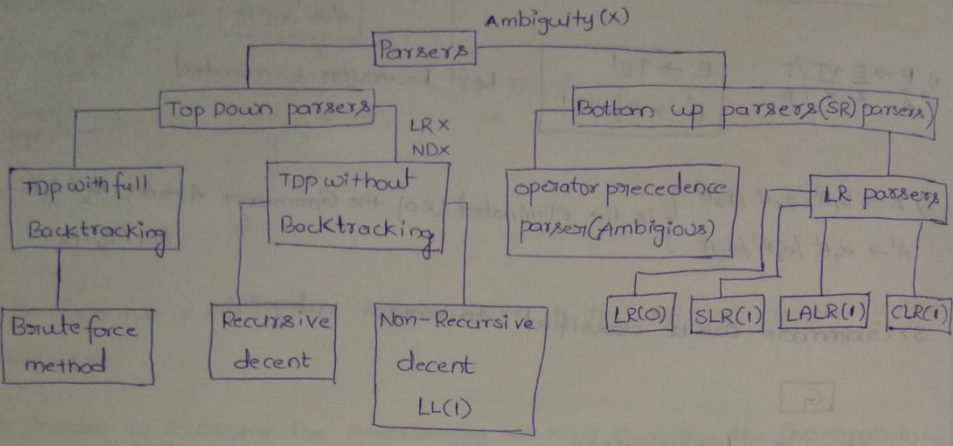
$B \rightarrow c/e$

$C \rightarrow d$

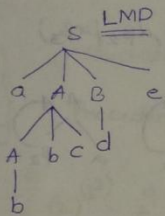
$D \rightarrow e$

⇒ Now, If n

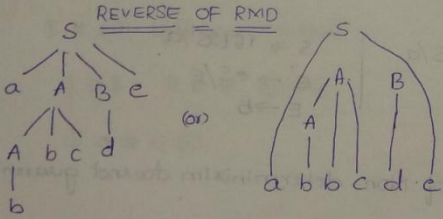
variable



⇒  
 $S \rightarrow aABe$   
 $A \rightarrow Abc/b$   
 $B \rightarrow d$   
 $w = abbade$



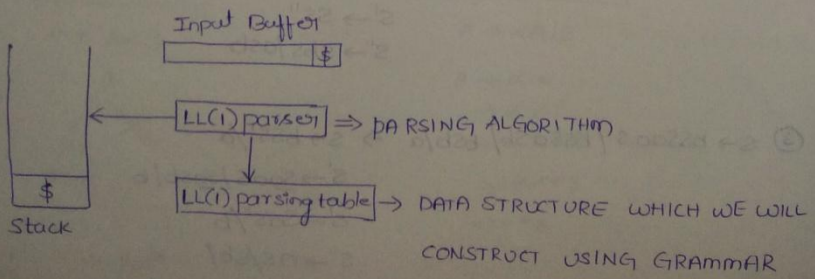
The main thing that we must assure is at every point when we have more than two productions to be chosen, which one to choose"



⇒ The main decision that should be made is if I see a terminal when to Reduce

## LL(1) PARSER / NON RECURSIVE DECENT PARSER

Left to Right, Left most Derivation, (1) = No. of look aheads



⑥

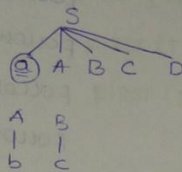
Now, Before constructing the LL(1) parsing table we should know two functions they are FIRST AND FOLLOW

⑦

FIRST():

$S \rightarrow a ABCD$

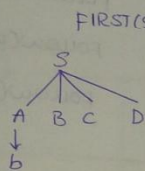
- $A \rightarrow b$
- $B \rightarrow c$
- $C \rightarrow d$
- $D \rightarrow e$



- $FIRST(S) = a$
- $FIRST(A) = b$
- $FIRST(B) = c$
- $FIRST(C) = d$
- $FIRST(D) = e$

$S \rightarrow ABCD$

- $A \rightarrow b$
- $B \rightarrow c$
- $C \rightarrow d$
- $D \rightarrow e$

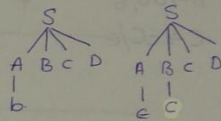


$FIRST(S) = b$

$S \rightarrow ABCD$

- $A \rightarrow b/e$
- $B \rightarrow c$  (small 'c')
- $C \rightarrow d$
- $D \rightarrow e$

$FIRST(S) = \{b, c\}$



FOLLOW():

⇒ what is the terminal which could follow a variable in the process of derivation.

⇒ follow of start symbol always contain '\$'

$S \rightarrow ABCD$

- $A \rightarrow b/e$
- $B \rightarrow c/e$
- $C \rightarrow d$
- $D \rightarrow e$

- $FOLLOW(S) = \{\$ \}$
- $FOLLOW(A) = FIRST(B, C, D) = \{c, d, e\}$
- $FOLLOW(B) = FIRST(C, D) = \{d, e\}$
- $FOLLOW(C) = FIRST(D) = \{e\}$

FOLLOW NEVER CONTAIN  
"EPSILON"

⇒ Now, If nothing is following a variable i.e. If nothing is at the RHS of a variable then the follow of that variable is the follow of LHS

$\therefore FOLLOW(D) = FOLLOW(S) = \{\$ \}$

EXAMPLES ON HOW TO FIND FIRST AND FOLLOW IN LL(1) PARSER (L-6)

CONSTRUCT

8

1)  $S \rightarrow ABCDE$   
 $A \rightarrow a/\epsilon$   
 $B \rightarrow b/\epsilon$   
 $C \rightarrow c$   
 $D \rightarrow d/\epsilon$   
 $E \rightarrow e/\epsilon$

$FIRST(S) = \{a, b, c\}$   
 $FIRST(A) = \{a, \epsilon\}$   
 $FIRST(B) = \{b, \epsilon\}$   
 $FIRST(C) = \{c\}$   
 $FIRST(D) = \{d, \epsilon\}$   
 $FIRST(E) = \{e, \epsilon\}$

$FOLLOW(S) = \{\$ \}$   
 $FOLLOW(A) = \{b, c\}$   
 $FOLLOW(B) = \{c\}$   
 $FOLLOW(C) = \{d, e, \$ \}$   
 $FOLLOW(D) = \{e, \$ \}$   
 $FOLLOW(E) = \{\$ \}$

17  
 $E \rightarrow TE'$   
 $E' \rightarrow +TE'/\epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT'/\epsilon$   
 $F \rightarrow id/\epsilon$

NOW THE

	id
E	$E \rightarrow TE$
E'	
T	$T \rightarrow FT$
T'	
F	$F \rightarrow$

2)  $S \rightarrow Bb/cd$   
 $B \rightarrow aB/\epsilon$   
 $C \rightarrow cC/\epsilon$

$FIRST(S) = \{a, b, c, d\}$   
 $FIRST(B) = \{a, \epsilon\}$   
 $FIRST(C) = \{c, \epsilon\}$

$FOLLOW(S) = \{\$ \}$   
 $FOLLOW(B) = \{b\}$   
 $FOLLOW(C) = \{d\}$

3)  $E \rightarrow TE'$   
 $E' \rightarrow +TE'/\epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT'/\epsilon$   
 $F \rightarrow id/\epsilon$

$FIRST(E) = \{id, c\}$   
 $FIRST(E') = \{+, \epsilon\}$   
 $FIRST(T) = \{id, c\}$   
 $FIRST(T') = \{*, \epsilon\}$   
 $FIRST(F) = \{id, c\}$

$FOLLOW(E) = \{\$, \}$   
 $FOLLOW(E') = \{\$, \}$   
 $FOLLOW(T) = \{+, \$, \}$   
 $FOLLOW(T') = \{+, \$, \}$   
 $FOLLOW(F) = \{*, +, \$, \}$

4)  $S \rightarrow ACB/\epsilon bB/ba$   
 $A \rightarrow da/BC$   
 $B \rightarrow gl/\epsilon$   
 $C \rightarrow h/\epsilon$

$FIRST(S) = \{e, d, g, h, b, a\}$   
 $FIRST(A) = \{d, g, h, \epsilon\}$   
 $FIRST(B) = \{g, \epsilon\}$   
 $FIRST(C) = \{h, \epsilon\}$

$FOLLOW(S) = \{\$ \}$   
 $FOLLOW(A) = \{h, g, \$ \}$   
 $FOLLOW(B) = \{g, a, h, g\}$   
 $FOLLOW(C) = \{g, \$, b, h\}$

5)  $S \rightarrow aABb$   
 $A \rightarrow C/\epsilon$   
 $B \rightarrow d/\epsilon$

$FIRST(S) = \{a\}$   
 $FIRST(A) = \{c, \epsilon\}$   
 $FIRST(B) = \{d, \epsilon\}$

$FOLLOW(S) = \{\$ \}$   
 $FOLLOW(A) = \{d, b\}$   
 $FOLLOW(B) = \{b\}$

6)  $S \rightarrow aBDh$   
 $B \rightarrow cC$   
 $C \rightarrow bc/\epsilon$   
 $D \rightarrow EF$   
 $E \rightarrow gl/\epsilon$   
 $F \rightarrow fl/\epsilon$

$FIRST(S) = \{a\}$   
 $FIRST(B) = \{c\}$   
 $FIRST(C) = \{b, \epsilon\}$   
 $FIRST(D) = \{g, b, \epsilon\}$   
 $FIRST(E) = \{g, \epsilon\}$   
 $FIRST(F) = \{f, \epsilon\}$

$FOLLOW(S) = \{\$ \}$   
 $FOLLOW(B) = \{g, b, h\}$   
 $FOLLOW(C) = \{g, b, h\}$   
 $FOLLOW(D) = \{h\}$   
 $FOLLOW(E) = \{f, h\}$   
 $FOLLOW(F) = \{h\}$

2)  $S \rightarrow (S)$

S	S
---	---

Now,  $w =$

CONSTRUCTION OF LL(1) PARSING TABLE (L-7)

9

8

$E \rightarrow TE'$	FIRST(E) = {id, c}	FOLLOW(E) = { $\$, \}$ }
$E' \rightarrow +TE' / \epsilon$	FIRST(E') = {+, $\epsilon$ }	FOLLOW(E') = { $\$, \}$ }
$T \rightarrow FT'$	FIRST(T) = {id, c}	FOLLOW(T) = {+, $\$, \}$ }
$T' \rightarrow *FT' / \epsilon$	FIRST(T') = {*, $\epsilon$ }	FOLLOW(T') = {+, $\$, \}$ }
$F \rightarrow id / (E)$	FIRST(F) = {id, c}	FOLLOW(F) = {*, +, $\$, \}$ }

NOW THE LL(1) PARSING TABLE LOOKS LIKE

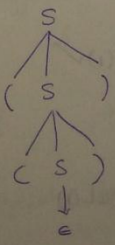
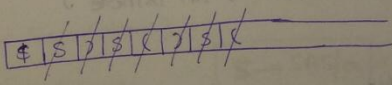
	id	+	*	(	)	$\$$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

$\Rightarrow S \rightarrow (S) / \epsilon$

All Grammars are not feasible for LL(1) parsing.

	(	)	$\$$
S	$S \rightarrow (S)$	$S \rightarrow \epsilon$	$S \rightarrow \epsilon$

Now,  $w = (( )) \ \$$



ANY GRAMMAR WHICH IS LEFT RECURSIVE/NO CANNOT BE USED FOR LL(1) PARSING

Non-deterministic

CHECK WHETHER THE GRAMMARS ARE LL(1) OR NOT

1)  $S \rightarrow asbs / bsas / \epsilon$   
 $\{a\} \{b\} \{a, b, \epsilon\} \Rightarrow$  Not LL(1)

$\hookrightarrow$  which means the production must be placed under 's' row and 'a' column.

$\hookrightarrow$  since the  $S \rightarrow \epsilon$  production should be placed under the follow(s) which are  $\{a, b\}$ , we have already placed production in 's' row and 'a' column which means a single CELL has more than one entry, so the grammar is not LL(1) X

2)  $S \rightarrow aABb \Rightarrow \{a\}$   
 $A \rightarrow c \mid \epsilon \Rightarrow \{c\}$  and follow(A) =  $\{d, b\}$   
 $B \rightarrow d \mid \epsilon \Rightarrow \{d\}$  and  $\{b\} \Rightarrow$  IS LL(1) ✓

$\hookrightarrow$  Conflict

3)  $S \rightarrow A/a$   $\{a\} \{a\} =$  Not LL(1) X  
 $A \rightarrow a \quad \{a\}$

4)  $S \rightarrow aB \mid \epsilon \quad \{a\} \{b\} \Rightarrow$  Not X<sup>n</sup>  
 $B \rightarrow bC \mid \epsilon \quad \{b\} \{b\} \Rightarrow$  NO X<sup>n</sup>  
 $C \rightarrow cS \mid \epsilon \quad \{c\} \{b\} \Rightarrow$  NO X<sup>n</sup> } LL(1) ✓

5)  $S \rightarrow AB$   
 $A \rightarrow a \mid \epsilon \Rightarrow \{a\} \{b, \epsilon\} \Rightarrow$  NO X<sup>n</sup>  
 $B \rightarrow b \mid \epsilon \Rightarrow \{b\} \{b\} \Rightarrow$  NO X<sup>n</sup> } LL(1) ✓

6)  $S \rightarrow aSA \mid \epsilon \Rightarrow \{a\} \{c, \epsilon\} \Rightarrow$  NO X<sup>n</sup>  
 $A \rightarrow c \mid \epsilon \Rightarrow \{c\} \{c\} \Rightarrow$  X<sup>n</sup> is there } X

7)  $S \rightarrow A$   
 $A \rightarrow Bb \mid cd \Rightarrow \{a, b\} \{c, d\}$   
 $B \rightarrow aB \mid \epsilon \Rightarrow \{a\} \{b\}$   
 $C \rightarrow cC \mid \epsilon \Rightarrow \{c\} \{d\}$  } LL(1) ✓

8)  $S \rightarrow iEtss/a \quad \{i\} \{a\}$   
 $s \rightarrow es \mid \epsilon \quad \{e\} \{e\}$  } Not LL(1) X  
 $E \rightarrow b$

8)  $S \rightarrow aAa \mid \epsilon \quad \{a\} \{a, a\}$  X NOT LL(1)  
 $A \rightarrow abS \mid \epsilon$

RECURSIVE

$E \rightarrow iE'$   
 $E' \rightarrow +iE'/\epsilon$

$\Rightarrow$  The parser we are going

$E()$   
 $\{$   
 1 if (l =  
 2 {

$\{$   
 $l = \text{getchar}()$

main()  
 $\{$   
 1)  $E()$   
 2) if (l =  
 3) printf(  
 $\}$

OPERATOR

OPERATOR

A Grammar operator G  
 $\Rightarrow$  NO Two  
 $\Rightarrow$  NO eps

$\Rightarrow$  This p

# RECURSIVE DECENT PARSER (L-8)

$E \rightarrow iE'$   
 $E' \rightarrow +iE'/\epsilon$

The parser is called Recursive Decent parser because for every variable we are going to write Recursive functions.

```

E()
{
    1) if (l == 'i')
    2) {
        match('i');
    3) E';
}
l = getch();
}

E'()
{
    1) if (l == '+')
    2) match('+');
    3) match('i');
    4) E'();
    5) else return;
}

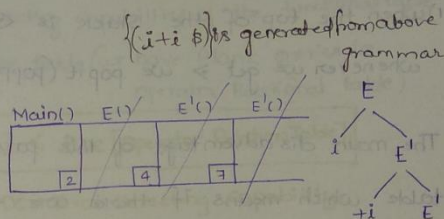
match(char t)
{
    if (l == t)
        l = getch();
    else
        printf("error");
}
    
```

main()

```

{
    1) E()
    2) if (l == '$')
    3) printf("parsing success");
}
    
```

⇒ This parser uses Recursion stack for parsing.  
 ⇒ Here l = look Ahead



# OPERATOR GRAMMAR AND OPERATOR PRECEDENCE PARSER (L-9)

## OPERATOR GRAMMAR

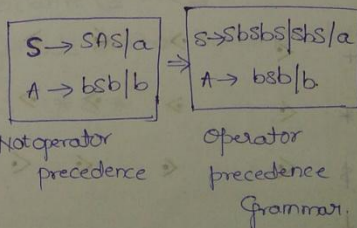
A Grammar that is used to define the mathematical operations is called operator Grammar (with some Restrictions)

- ⇒ NO Two variables must be Adjacent
- ⇒ No Epsilon productions

$E \rightarrow E + E / E * E / id$  (✓)

$E \rightarrow EAE / id$   
 $A \rightarrow + / *$  } Not operator Grammar

⇒ This parser parses the Ambiguous grammars by creating operator Relation



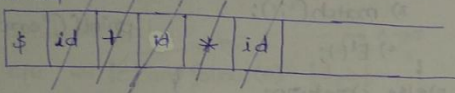
Not LL(1) X

The operator Relational table looks like

	id	+	*	\$
id	-	>	>	>
+	<	>	<	<
*	<	>	>	>
\$	<	<	<	⊖

W = id + id \* id \$

↑ ↑ ↑ ↑  
look head



Now The Algorithm goes like this

- 1) when the top of the Stack is < than the lookAhead then push it and whenever we get > we pop it (popping means actually we Reduced it)

The main disadvantage of this parser is the size of the operator Relational table which means if there are 4 operators then size of the table is 16 (4<sup>2</sup>) and if there are 5 operators then there would be 25 entries (5<sup>2</sup>). So Generally if there are 'n' operators, the size of the table is  $O(n^2)$

### OPERATOR GRAMMAR AND OPERATOR PRECEDENCE PARSER

Now, To reduce the size of the table we use operator function table

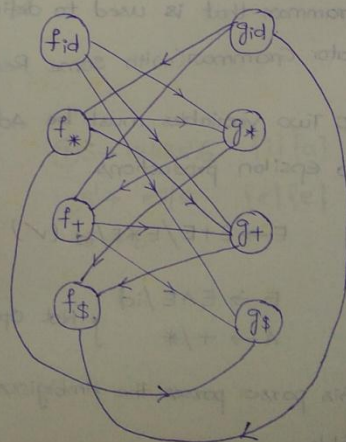
	id	+	*	\$	→ function 'G'
id	-	>	>	>	

+	<	>	<	>
*	<	>	>	>
\$	<	<	<	<

Function (F)

$$\triangleright = F_{id} \rightarrow G_{id} (F \rightarrow G)$$

$$\triangleleft = G_{id} \rightarrow F_{id} (G \rightarrow F)$$

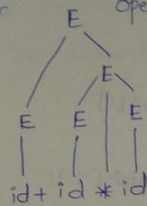


The given grammar is

$$E \rightarrow E + E / E * E / id$$

⇒ id will have higher precedence than any other operator

⇒ '\$' will have least precedence than any other operator



⇒ Top of the stack will be '\$'.

Now, the Lor

Now, the L

Similarly fr

Now if in

∴ The Siz

⇒ In the

nothing bu

is less th

ED

2) P<sub>i</sub> → SR/S

R → bSR

S → wbs

w → L\*

L → id

id

\*

b

\$

Now, the longest path from fid is  $f_{id} \rightarrow g_* \rightarrow f_+ \rightarrow g_+ \rightarrow f_\$$  13

Now, the longest path from gid is  $g_{id} \rightarrow f_* \rightarrow g_* \rightarrow f_+ \rightarrow g_+ \rightarrow f_\$$

Similarly find the longest paths from each node the function table looks like

	id	+	*	\$	
f	4	2	4	0	$f_{id} \xrightarrow{1} g_* \xrightarrow{2} f_+ \xrightarrow{3} g_+ \xrightarrow{4} f_\$ = 4$ $\xrightarrow{1} f_+ \xrightarrow{2} g_+ \xrightarrow{3} f_\$ = 2$
g	5	1	3	0	

Now if indeed to compare  $(+, +) \Rightarrow f_+ \quad g_+$   
 $\Rightarrow 2 \quad 1 \Rightarrow 2 > 1 \Rightarrow (+ > +)$

$\therefore$  The Size of the table =  $O(2^n)$   $n = \text{no. of operators}$ .

$\Rightarrow$  In the functional table, we don't have blank entries (Blank entries are nothing but errors) so, the error detecting capability of the functional table is less than that of operator relation table (we have blank entries in operator relation table)

$$\text{EDC} [\text{Operator Functional Table}] < \text{EDC} [\text{Operator Relation Table}]$$

EDC = Error Detecting Capability.

2)  $P \rightarrow SR/S$

$R \rightarrow bSR/bs$

$S \rightarrow wbs/w$

$w \rightarrow L*w/L$

$L \rightarrow id$

$P \rightarrow SbP/Sbs/S$

$S \rightarrow wbs/w$

$w \rightarrow L*w/L$

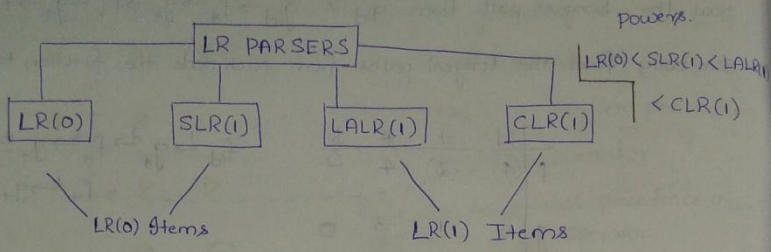
$L \rightarrow id$

	id	*	b	\$
id	-	>	>	>
*	<	<	>	>
b	<	<	<	>
\$	<	<	<	-

$\Rightarrow$  Here \* is defined as Right Associative ( $w \rightarrow L*w$ ) so the Right side star has highest precedence

$$\therefore * < *$$

LR PARSING, LR(0) ITEMS AND LR(0) PARSING TABLE (L-10)



1)  $S \rightarrow AA$   
 $A \rightarrow aA/b$  } In LR parsers we have CLOSURE and GOTO Operations

The Augmented Grammar is  $S' \rightarrow S$   
 $S \rightarrow AA$   
 $A \rightarrow aA/b$

Any production with a dot in the RHS is called an item.

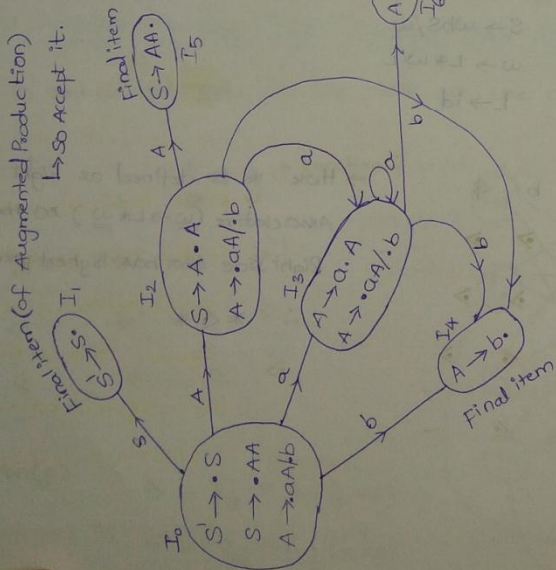
The LR(0) parsing tree is,

$S' \rightarrow S$   
 $S \rightarrow AA$  ①  
 $A \rightarrow aA/b$  ② ③

The parsing table is

ACTION	GOTO	
	A	S
a	$S_3$	1
b	$S_4$	2
$\$$	Accept	5
$R_1$	$R_2$	6
$R_3$	$R_4$	
$R_5$	$R_6$	

CANDIDATE COLLECTION OF LR(0) ITEMS



1. while writing the Reduce moves / while inspecting final items go to the productions and check

$S' \rightarrow S$   
 $S \rightarrow AA$  ①  
 $A \rightarrow aA$  ②  
 $A \rightarrow b$  ③

Now  $I_4$  is  $A \rightarrow b \cdot$  (3rd production)  $\Rightarrow I_4 \rightarrow R_3$

$R_1: S \rightarrow AA$   
 place  $R_1$  in follow  
 follow(S) = { $\$$ }

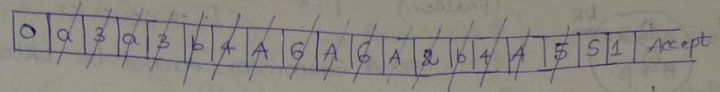
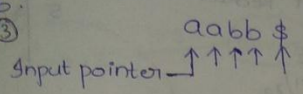
LR(0) PARSING

$S' \rightarrow S$   
 $S \rightarrow AA$  ①  
 $A \rightarrow aA/b$  ② ③

Always the  
 Initially I  
 at and as  
 and increm  
 Now top of  
 which stat  
 previous  
 Now  $S_n$  th  
 RHS of the  
 RHS. In thi  
 which me  
 then  
 onto the  
 it turns  
 = 6, 50  
 SLR(0)

LR(0) PARSING EXAMPLE AND SLR(1) TABLE (L-11)

$s' \rightarrow S$   
 $s \rightarrow AA$   
 $A \rightarrow aA/b$



- Always the top of the stack contains state (and first state will be zero)
- Initially  $I_0$  on 'a' is  $S_3$  which means shift the input you are looking at and as well as the state no on to the stack  $\Rightarrow$  [Input=a, State=3] = a|3 and increment the input pointer [continue]
- Now top of the stack is '4' and input pointer is b which means  $R_3$  which states that Reduce the production no.3. which means reduce the previous 'b'. (previous symbol).  $\hookrightarrow (A \rightarrow b)$
- Now in the stack how could we make Reduce move is look the RHS of the production that must be Reduced, and find the length of RHS in this example 'A  $\rightarrow$  b' is the production  $\Rightarrow$  length of RHS = 1 ( $\because |b|=1$ ) which means pop 2 symbols (x2) from stack. (if the length of RHS is 'x' then pop '2x' elements from stack) and push the LHS symbol onto the stack, and see the stack for the last used state number it turns out that it is '3' and look what '3' on 'A' is generating = 6, so push '6' onto the stack. when we see reduce moves we don't increment input pointer.

SLR(1)

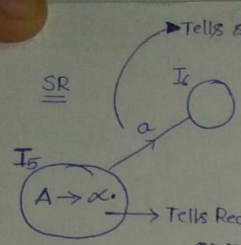
	ACTION			GOTO	
	a	b	\$	A	S
0	S3	S4		2	1
			accept		
1					
2	S3	S4		5	
3	S3	S4		6	
4	R3	R3	R3		
5					
6	R2	R2	R2		

$R_1: S \rightarrow AA$   
 place  $R_1$  in follow(s)  
 follow(s) = { \$ }

place the Reduce moves if the next Symbol is in the follow of current Symbol, this is the main difference between the LR(0) and SLR(1) parsers

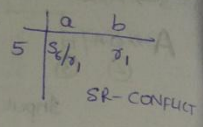
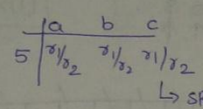
Now,  
 $R_3 \Rightarrow A \rightarrow b$  should be reduced  
 place  $R_3$  in follow(A) = { a, b, \$ }

$S \rightarrow A/a$   
 $A \rightarrow a$



LR(0)

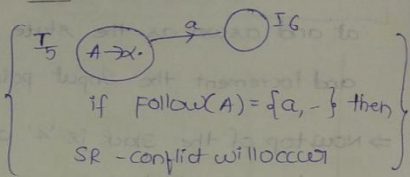
⇒ All the Grammars are not suitable for LR parsing due to shift Reduce conflicts.



⇒ A Grammar cannot be LR(0) if I have SR/RR conflicts.

EXAMPLES OF LR(0) AND SLR(1) (L-12)

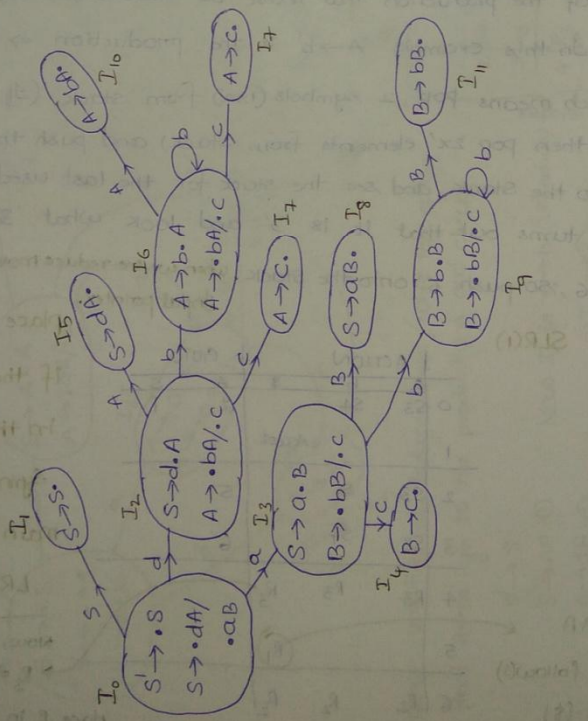
- 1)  $S \rightarrow dA/aB \{d, a\}$  → 1) LL(1) ✓
- 2)  $A \rightarrow bA/c \{bc\}$  → 2) LR(0) ✓
- 3)  $B \rightarrow bB/c \{bc\}$  → 3) SLR(1) ✓



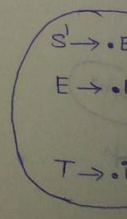
- ③  $S \rightarrow (L)/a$   
 $L \rightarrow L,S$

CANONICAL

CANONICAL COLLECTION OF LR(0) ITEMS



- ④  $E \rightarrow E + T$   
 $T \rightarrow i$



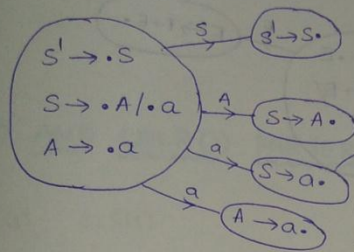
$S \rightarrow A/a \text{ for } \{a\}$   
 $A \rightarrow a$

Not LL(1) x  
 LR(0) x  
 SLR(1) x } Ambiguous Grammar

parsing

- CONFLICT

SR/RR



follow(S) = \$  
 follow(A) = \$ } Not SLR(1)

2 Reduce moves from the same state  
 RR-conflict so LR(0) x (if we get 2 reduce moves from the same state then the grammar is not LR(0))

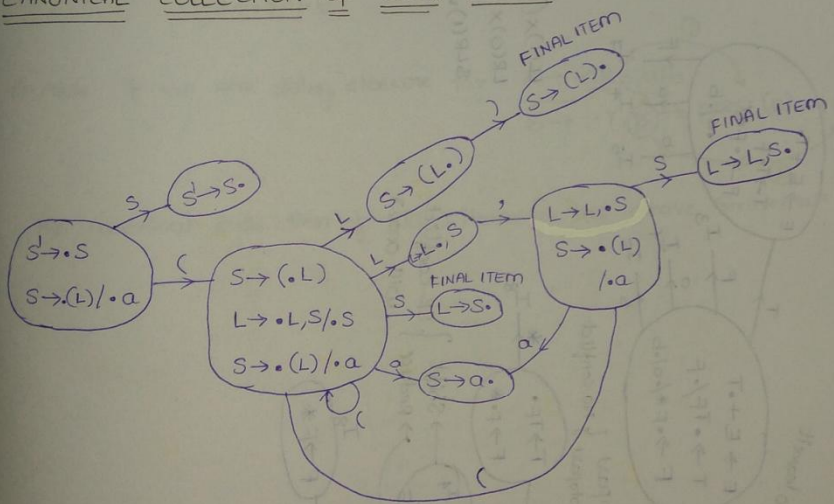
③  $S \rightarrow (L)/a$   
 $L \rightarrow L,S/S$

LL(1) x (Left Recursive)  
 LR(0) ✓  
 SLR(1) ✓

⇒ fail

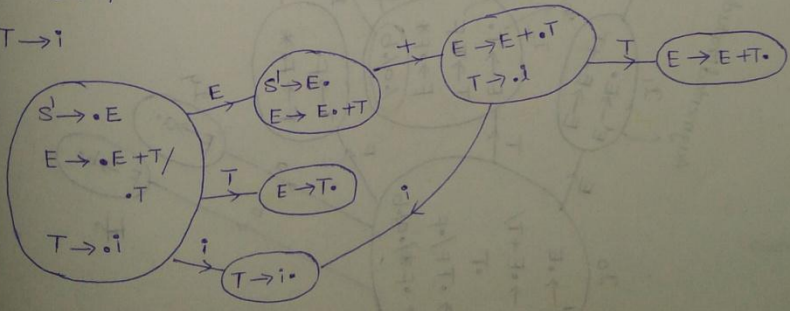
} then

CANONICAL COLLECTION OF LR(0) ITEMS

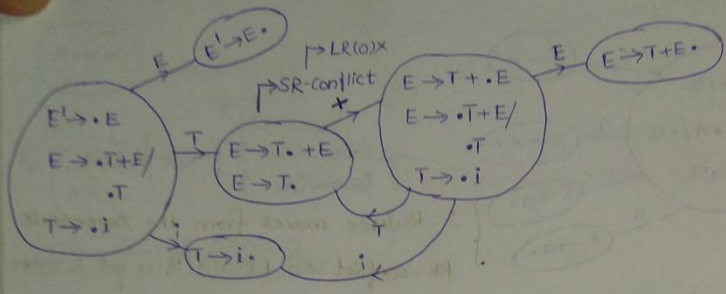


④  $E \rightarrow E+T/T$

$T \rightarrow i$

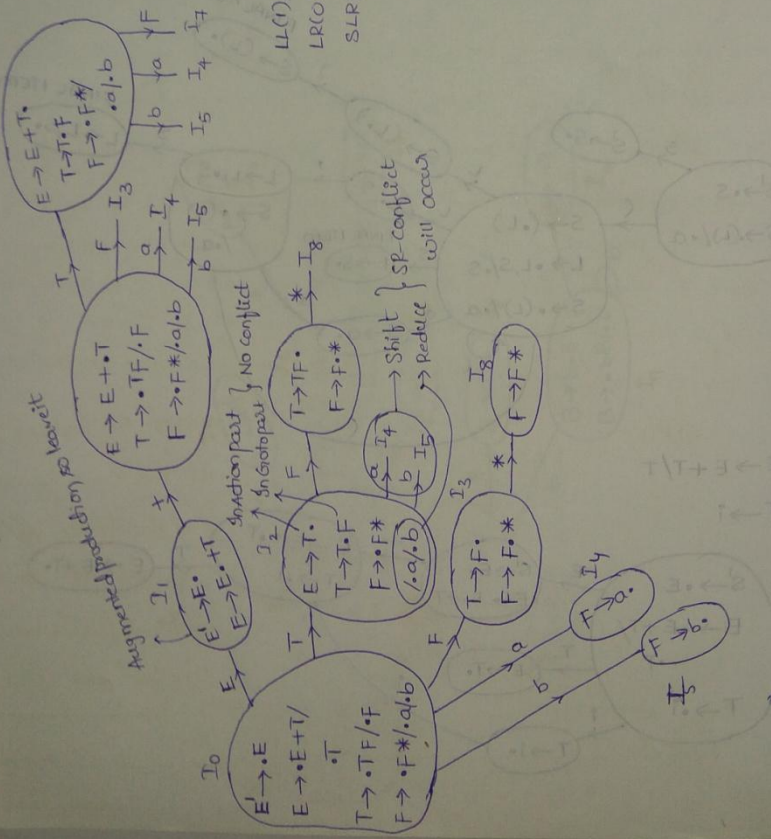


5)  $E \rightarrow T + E / T$        $LL(1) \times$        $\rightarrow$   $L$  is Right Associative      18  
 $T \rightarrow i$        $LR(0) \times$   
 $SLR(1) \checkmark$



6)  $E \rightarrow E + T$   
 $T \rightarrow T F / F$   
 $F \rightarrow F * a / b$

LR(1) (Left Recursive)  
 $LR(0) \times$   
 $SLR(1) \checkmark$



7)  $S \rightarrow AA$   
 $A \rightarrow E$   
 $B \rightarrow E$

CLR(1) AN

LALR(1)

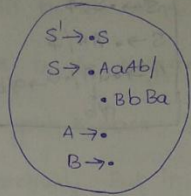
LR(1)

8)  $S \rightarrow AA$   
 $A \rightarrow OA/b$

In case if

The conc

7)  $S \rightarrow AaAb / BbBa \{a, b\}$  LL(1)  $\checkmark$   
 $A \rightarrow \epsilon$  LR(0)  $\times$   
 $B \rightarrow \epsilon$  SLR(1)  $\times$



	a	b	\$
0	$r_3 / r_4$	$r_3 / r_4$	

RR-Conflict

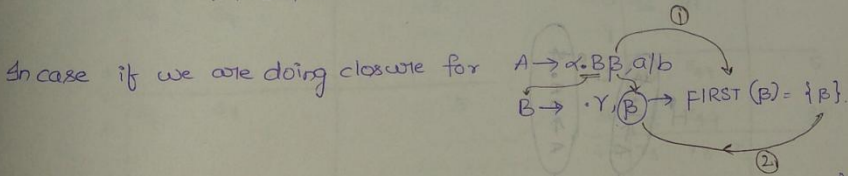
CLR(1) AND LALR(1) PARSERS L-14

LALR(1) CLR(1)

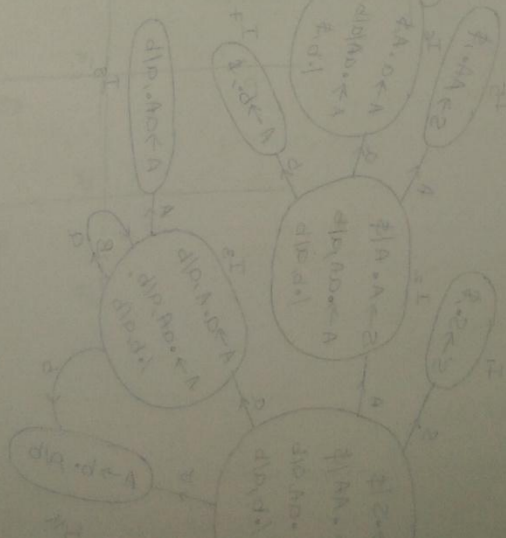
LR(1) Items = LR(0) items + lookahead

1)  $S \rightarrow AA$   
 $A \rightarrow aA / b$

$S' \rightarrow \cdot S$  is the augmented Grammar  
 $S \rightarrow \cdot AA$   
 $A \rightarrow \cdot aA / \cdot b$



The canonical collection of LR(1) items for the above Grammar is



Augmented Grammar

$S \rightarrow \cdot S, \$$   
 $S \rightarrow \cdot AA / \$$   
 $A \rightarrow \cdot aA / \cdot b \rightarrow a/b$   
 $\quad \quad \quad \downarrow$   
 $\quad \quad \quad a/b$

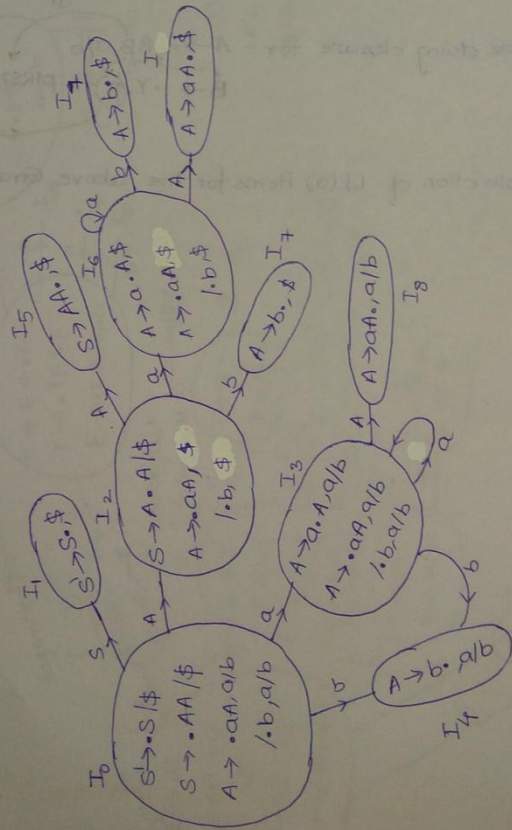
look ahead is always \$ for Augmented production.

(20)

LR(0) AND LALR(1) PARSERS L-11

LR(0) Items = LR(0) Items + Lookahead

CANONICAL COLLECTION OF LR(0) ITEMS



=> The Goto  
 tables,  
 In the  
 the fol  
 are ge

=> from th  
 look head  
 => Sim lar  
 Look ab

CLR(1)

- 1
- 2
- 3
- 4
- 5
- 6
- 7
- 8
- 9

$I_2, I_6 \Rightarrow$   
 $I_4, I_7 \Rightarrow$   
 $I_8, I_9 \Rightarrow$

No of sta

for Augmented

(20)

⇒ The Goto part and shift part will be the same as LR(0), SLR(1) parsing tables, the main difference arises in the placement of the final items  
 In the LR(0) and SLR(1) we are going to place in the entire row and the follow of LHS (in SLR(1)) respectively. But in CLR and LALR(1) we are going to place the reduce moves only in look ahead symbols.

⇒ from the above diagrams  $[I_3, I_6]$  have same LR(0) items but differ in look heads

⇒ Similarly  $[I_4, I_7], [I_8, I_9]$  also have same LR(0) items but differ in look aheads.

CLR(1) PARSING TABLE

	a	b	\$	S	A
0	S <sub>3</sub>	S <sub>4</sub>			2
1					
2	S <sub>6</sub>	S <sub>7</sub>			5
3	S <sub>3</sub>	S <sub>4</sub>			8
4	r <sub>3</sub>	r <sub>3</sub>			
5			r <sub>1</sub>		
6	S <sub>6</sub>	S <sub>7</sub>			9
7			r <sub>3</sub>		
8	r <sub>2</sub>	r <sub>2</sub>			
9			r <sub>2</sub>		

LALR(1) TABLE

	a	b	\$	S	A
0	S <sub>36</sub>	S <sub>47</sub>			2
1					
2	S <sub>36</sub>	S <sub>47</sub>			5
3	S <sub>36</sub>	S <sub>47</sub>			89
4	r <sub>3</sub>	r <sub>3</sub>	r <sub>3</sub>		
5			r <sub>1</sub>		
6	S <sub>36</sub>	S <sub>47</sub>			9
7			r <sub>3</sub>		
8	r <sub>2</sub>	r <sub>2</sub>			
9			r <sub>2</sub>		

$[I_3, I_6] \Rightarrow I_{36}$

$[I_4, I_7] \Rightarrow I_{47}$

$[I_8, I_9] \Rightarrow I_{89}$

$[No\ of\ states\ in\ CLR(1)] \geq [No\ of\ states\ in\ SLR(1)] = [No\ of\ states\ in\ LALR(1)] = [No\ of\ states\ in\ LR(0)]$

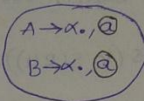
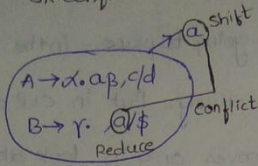
(21)

# CONFLICTS AND EXAMPLES OF CLR(1) AND LALR(1) (L-15) 20

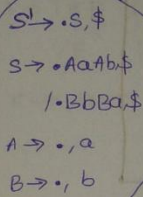
SR conflict

RR conflict

LR(1) items

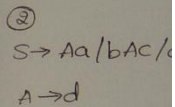
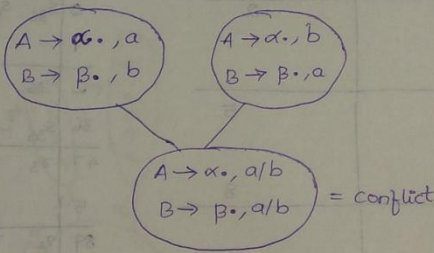


LR(0) items



⇒ If the grammar is not CLR(1) then the Grammar is not LALR(1) because we reduce the size of the table but not the conflicts in LALR(1) parser

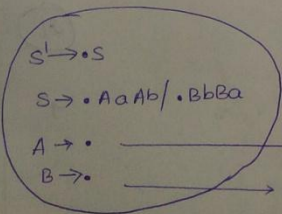
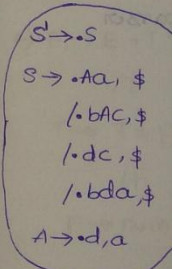
⇒ If the Grammar is CLR(1) then it may or maynot be LALR(1)



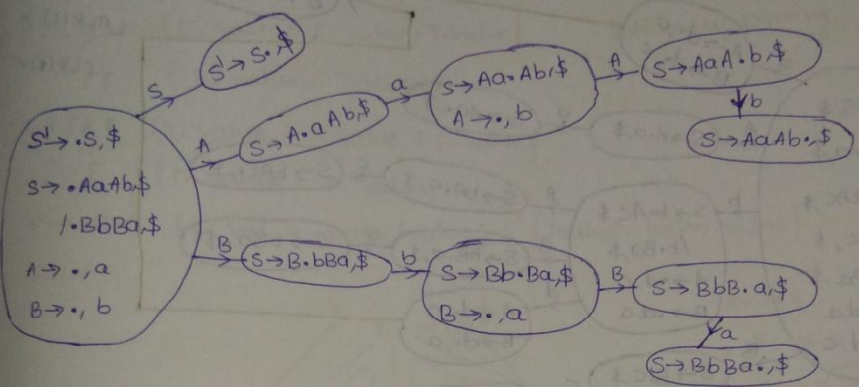
i)  $S \rightarrow AaAb / BbBa$

$A \rightarrow \epsilon$   
 $B \rightarrow \epsilon$

- LL(1) X
- LR(0) X
- SLR(1) X
- CLR(1) ✓
- LALR(1) ✓



placed under follow of  $A = \{a, b\}$   
 placed under follow of  $B = \{a, b\}$  } ⇒ Not SLR(1)

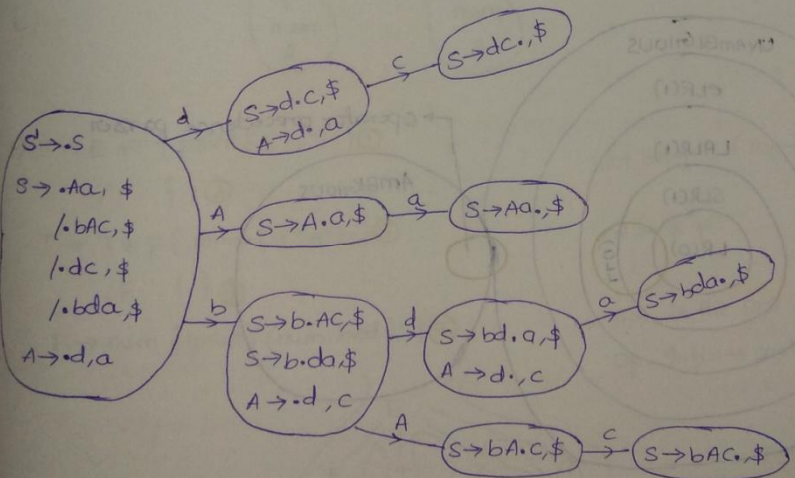


because  
parser

②

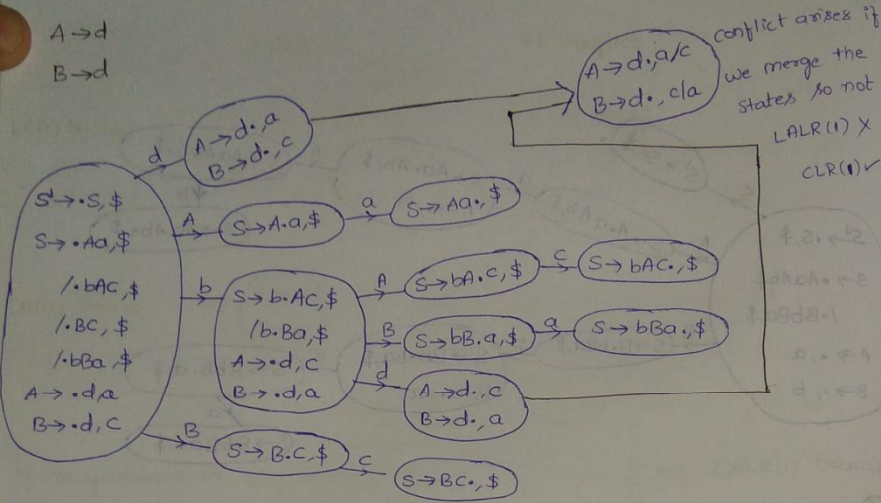
$S \rightarrow Aa/bAc/dc/bda$   
 $A \rightarrow d$

- LL(1) X
- LR(0) X
- SLR(1) X
- CLR(1) ✓
- LALR(1)

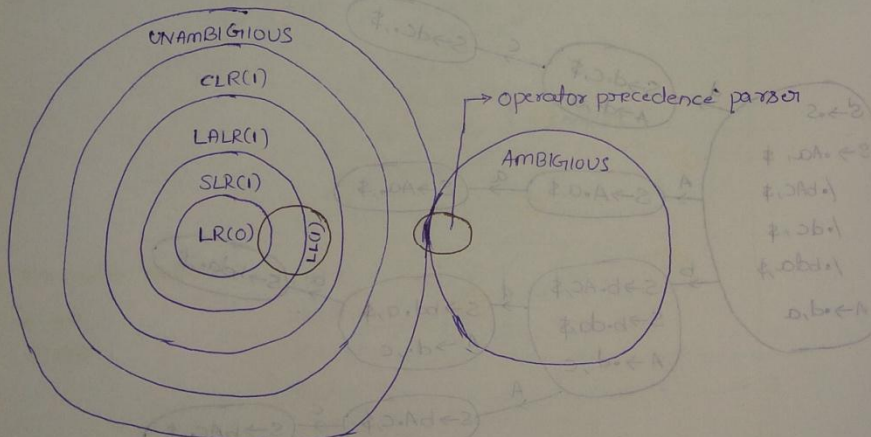


③  $S \rightarrow Aa/bAC/BC/bBa$

$A \rightarrow d$   
 $B \rightarrow d$



COMPARISON OF THE PARSERS (L-16)



⇒ Every Grammar which is LL(1) is definitely LALR(1)

SYNTAX DIRE

⇒ Grammar +

- 1)  $E \rightarrow E+T \{E, T\}$
- $T \rightarrow T * F \{T, F\}$
- $F \rightarrow \text{num} \{F\}$

# SYNTAX DIRECTED TRANSLATION (L-17)

25

⇒ Grammar + Semantic Rules = SDT

1)  $E \rightarrow E + T$  { E.value = E.value + T.value }

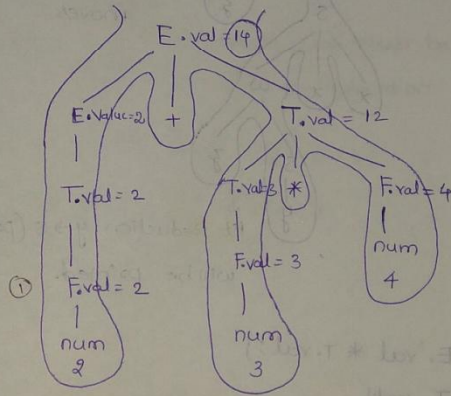
    / T { E.value = T.value }

$T \rightarrow T * F$  { T.value = T.value \* F.value }

    / F { T.value = F.value }

$F \rightarrow \text{num}$  { F.val = num.lvalue } { lvalue = lexicon value }

Bottom-up parsing.



$$\begin{aligned} &2 + 3 * 4 \\ &= 2 + (3 * 4) \\ &= 2 + 12 = 14 \end{aligned}$$

2)  $E \rightarrow E + T$  { printf(" + "); } ①

    / T { } ②

$T \rightarrow T * F$  { printf(" \* "); } ③

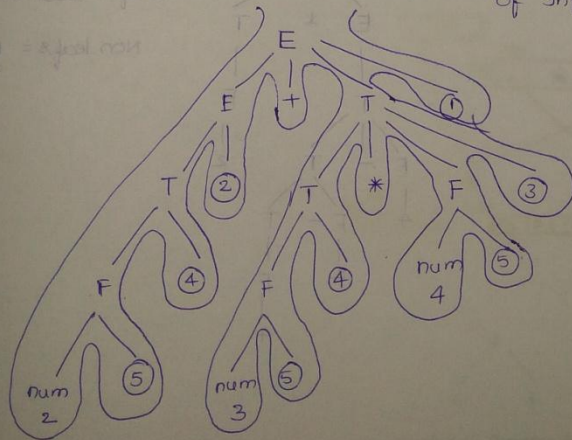
    / F { } ④

$F \rightarrow \text{num}$  { printf(num.lval); } ⑤

2 + 3 \* 4 (Top-down parser)

2 3 4 \* +

⇒ This is the SDT for conversion of infix to postfix expression



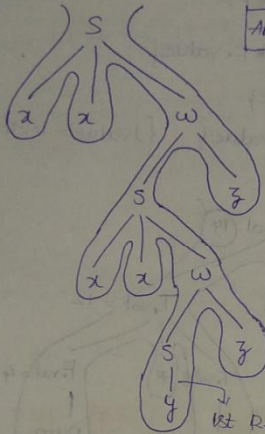
Top down  
parsing

conflict arises if we merge the states, so not LALR(1) X CLR(1) ✓

answer

③  $S \rightarrow xxw \{ \text{printf}(1); \}$   
 $\quad \quad \quad /y \quad \{ \text{printf}(2); \}$   
 $\quad \quad \quad w \rightarrow Sz \quad \{ \text{printf}(3); \}$

string xxxzyzz



Ans: 2 3 1 3 1

⇒ Carry the action on Reduce moves

1st Reduction  $y \rightarrow S$  ( $\text{printf}(2)$ ); 'S02' will be printed.

④

$E \rightarrow E * T \{ E.val = E.val * T.val; \}$

$\quad \quad \quad /T \quad \{ E.val = T.val; \}$

$T \rightarrow F - T \{ T.val = F.val - T.val; \}$

$\quad \quad \quad /F \quad \{ T.val = F.val; \}$

$F \rightarrow 2 \quad \{ F.val = 2; \}$

$\quad \quad \quad /4 \quad \{ F.val = 4; \}$

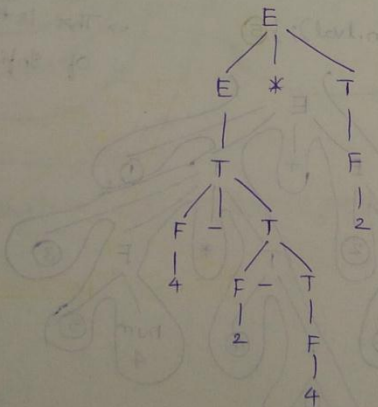
$w = 4 - 2 - (4 * 2)$

$w = (4 - (2 - 4)) * 2$

$= (4 - (-2)) * 2$

$= (4 + 2) * 2$

$= \underline{\underline{12}}$



No. of Reductions = No. of

Non leafs = 10

⑤  $E \rightarrow E \# T$   
 $\quad \quad \quad /T$   
 $T \rightarrow T \& F$   
 $\quad \quad \quad /F$   
 $F \rightarrow \text{num}$

$w = 2 \# 3 \& 5$

$= 2 * 3 + 5$

$= ((2 * 3) + 5)$

$= (6 + 30)$

$= \underline{\underline{40}}$

L-18

SDT TO BUILD

⑥  $E \rightarrow E_1 + T \{ F \}$

$\quad \quad \quad /T \quad \{ F \}$

$T \rightarrow T_1 * F \{ F \}$

$\quad \quad \quad /F \quad \{ F \}$

$F \rightarrow \text{id} \{ F \}$

$w = 2 + 3 * 4$

$E \text{ ptr} = 100$

$T \text{ ptr} = 100$

$F \text{ ptr} = 100$

Cont

$E \rightarrow E \# T \{ E.val = E.val * T.val; \}$   
 $\quad / T \quad \{ E.val = T.val \}$   
 $T \rightarrow T \& F \{ T.val = T.val + F.val \}$   
 $\quad / F \quad \{ T.val = F.val \}$   
 $F \rightarrow num \quad \{ F.val = num.value; \}$

$w = 2 \# 3 \& 5 \# 6 \& 4$  what is the output

~~$= 2 * 3 + 5 * 6 + 4$   
 $= ((2 * 3) + (5 * 6) + 4)$   
 $= (6 + 30 + 4)$   
 $= \underline{40}$~~

wrong because '+' is defined at highest level (Bottom level) and must be evaluated first and then multiplication must be evaluated.

$\Rightarrow 2 * (3 + 5) * (6 + 4)$   
 $= 2 * (8) * (10)$   
 $= \underline{160} \checkmark$

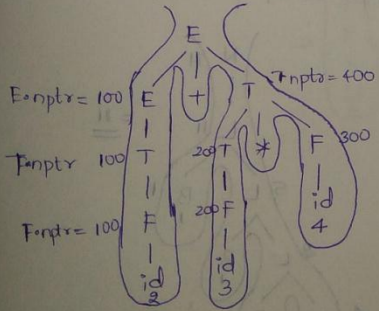
L-18

SDT TO BUILD SYNTAX TREE

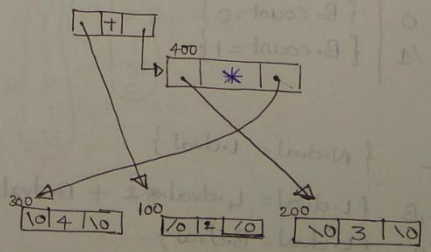
$E \rightarrow E_1 + T \{ E.nptr = mknode(E_1.nptr, '+', T.nptr); \}$   
 $\quad / T \quad \{ E.nptr = T.nptr; \}$   
 $T \rightarrow T_1 * F \{ T.nptr = mknode(T_1.nptr, '*', F.nptr); \}$   
 $\quad / F \quad \{ T.nptr = F.nptr; \}$   
 $F \rightarrow id \quad \{ F.nptr = mknode(null, id.name, null); \}$

Returns Address  
 $mknode = \text{make node}$   
 $nptr = \text{node pointer}$

$w = 2 + 3 * 4$



Concrete Syntax tree



Abstract Syntax tree

⑦ SDT FOR TYPE CHECKING

$E \rightarrow E_1 + E_2 \{ \text{if } ((E_1.type == E_2.type) \&\& (E_1.type == \text{int})) \text{ then } E.type = \text{int} \text{ else error} \}$

$/E_1 == E_2 \{ \text{if } ((E_1.type == E_2.type) \&\& (E_1.type == \text{int} / \text{boolean})) \text{ then } E.type = \text{boolean} \text{ else error} \}$

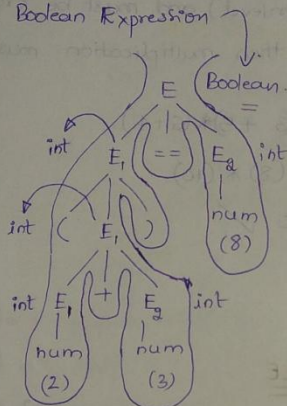
$(E_1) \{ E.type = E_1.type \}$

$/\text{num} \{ E.type = \text{int}; \}$

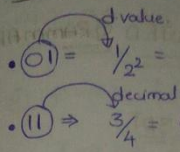
$/\text{True} \{ E.type = \text{boolean}; \}$

$/\text{false} \{ E.type = \text{boolean}; \}$

$w = \{ (2+3) == 8 \} = \text{Boolean Expression}$



L-19 S-ATT



⑩  $N \rightarrow L_1 L_2$

$L \rightarrow LB/B$

$B \rightarrow 0$

$/1$

SDT TO GENERATE

⑩  $S \rightarrow id = E$

$E \rightarrow E_1 + T$

$/T$

$T \rightarrow T_1 * F$

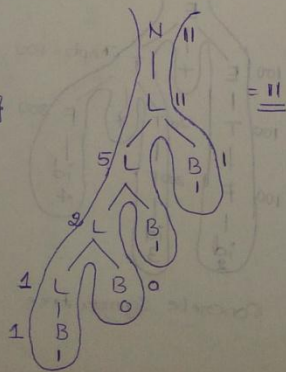
$/F$

$F \rightarrow id$

	<u>count</u> <u>all 1's</u>
$N \rightarrow L$	$\{ N.count = L.count \}$
$L \rightarrow L_1 B$	$\{ L.count = L_1.count + B.count \}$
$/B$	$\{ L.count = B.count \}$
$B \rightarrow 0$	$\{ B.count = 0 \}$
$/1$	$\{ B.count = 1 \}$

	<u>count</u> <u>all 0's</u>	No. of B's
$\Rightarrow$	$\Rightarrow$	
$\Rightarrow$	$\Rightarrow$	
$\Rightarrow$	$\Rightarrow$	
	$\{ B.count = 1 \}$	$\{ B.count = 1 \}$
	$\{ B.count = 0 \}$	$\{ B.count = 1 \}$

$N \rightarrow L$	$\{ N.dval = L.dval \}$
$L \rightarrow L_1 B$	$\{ L.dval = L_1.dval * 2 + B.dval \}$
$/B$	$\{ L.dval = B.dval \}$
$B \rightarrow 0$	$\{ B.dvalue = 0 \}$
$/1$	$\{ B.dvalue = 1 \}$



$w = 1011$

L-19 S-ATTRIBUTED AND L-ATTRIBUTED DEFINITIONS (21)

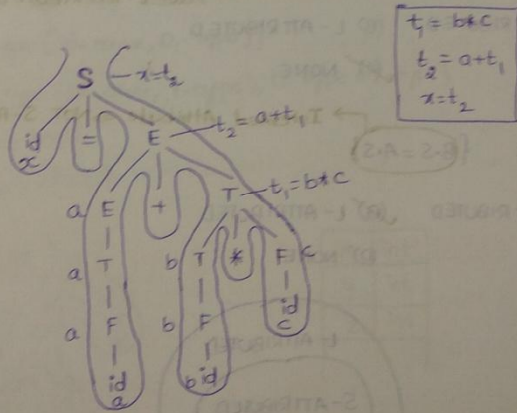
$\textcircled{I} \Rightarrow \frac{1}{2} = 0.25$  (value)  
 $\textcircled{II} \Rightarrow \frac{3}{4} = 0.75$  (decimal value)

$\textcircled{III} \rightarrow L_1, L_2$   
 $L \rightarrow L_1/B/B$   
 $B \rightarrow 0$   
 $\quad /1$

$\{ \text{L.dval} = L_1.\text{dval} + (L_2.\text{dval} / 2^{\text{L.count}}) \}$   
 $\{ \text{L.dvalue} = \{ L_1.\text{dval} + B.\text{dval} \} \}$   
 $\{ \text{L.count} = L_1.\text{count} + B.\text{count} \}$   
 $\{ \text{L.count} = B.\text{count} \}$   
 $\{ \text{L.dval} = B.\text{dvalue} \}$   
 $\{ B.\text{count} = 1, B.\text{dvalue} = 0 \}$   
 $\{ B.\text{count} = 1, B.\text{dvalue} = 1 \}$

Syntax TO GENERATE THREE ADDRESS CODE

- $\textcircled{I} \ S \rightarrow \text{id} = E \quad \{ \text{gen}(\text{id.name} = E.\text{place}); \}$   
 $E \rightarrow E_1 + T \quad \{ E.\text{place} = \text{newTemp}(); \text{gen}(E.\text{place} = E_1.\text{place} + T.\text{place}); \}$   
 $\quad / T \quad \{ E.\text{place} = T.\text{place}; \}$   
 $T \rightarrow T_1 * F \quad \{ T.\text{place} = \text{newTemp}(); \text{gen}(T.\text{place} = T_1.\text{place} * F.\text{place}); \}$   
 $\quad / F \quad \{ T.\text{place} = F.\text{place}; \}$   
 $F \rightarrow \text{id} \quad \{ F.\text{place} = \text{id.name}; \}$



DIFFERENCE BETWEEN S-ATTRIBUTED AND L-ATTRIBUTED SDT

S-ATTRIBUTED SDT

- 1) Uses only synthesized attributes
- 2) Semantic actions are placed at Right end of production  
 $A \rightarrow BC \{ \}$
- 3) Attributes are evaluated during Bottom up parsing

L-ATTRIBUTED SDT

- 1) Uses Both inherited and synthesized attributes. Each inherited attribute is restricted to inherit either from parent or Left siblings only.  
 Ex:  $A \rightarrow XYZ \{ y.S = A.S, y.S = X.S, y.S = Z.S \}$
- 2) Semantic Actions are placed anywhere on RHS  
 $A \rightarrow \{ \} BC$   
 $\quad \quad \quad /D \{ \} E$   
 $\quad \quad \quad /FG \{ \}$
- 3) Attributes are evaluated by traversing parse tree depth first left to Right

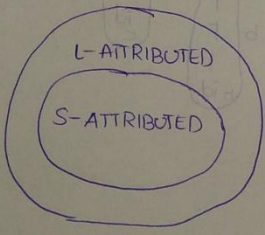
Inherited Attribute  
 ↑  
 Not S-ATTRIBUTED

- ①  $A \rightarrow LM \{ L.i = f(A,i); M.i = f(L,S); A.S = f(m,S); \}$
  - $A \rightarrow QR \{ R.i = f(A,i), Q.i = f(R,i); A.S = f(Q,S); \}$
- ↳ NOT L-ATTRIBUTED

- (A) S-ATTRIBUTED
- (B) L-ATTRIBUTED
- (C) BOTH
- (D) NONE

Inherited Attribute ⇒ NOT S-ATTRIBUTED

- ②  $A \rightarrow BC \{ B.S = A.S \}$
- (A) S-ATTRIBUTED
- (B) L-ATTRIBUTED
- (C) BOTH
- (D) NONE



SDT TO A

- ⑪  $D \rightarrow TL$
- $T \rightarrow int$
- $\quad \quad /ch$
- $L \rightarrow L_1$
- $\quad \quad /id$

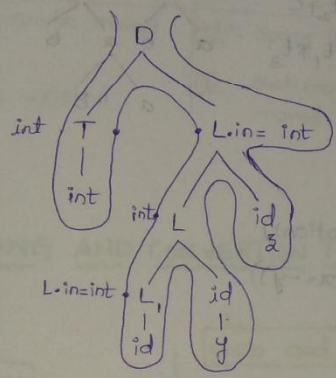
S-ATTRIB

- ⑫  $D \rightarrow D_1$
- $\quad \quad /T$
- $T \rightarrow in$
- $\quad \quad /ch$

SDT TO ADD TYPE INFORMATION INTO SYMBOL TABLE

- ⑩  $D \rightarrow TL \{L.in = T.type\} \Rightarrow$  Inherited Attribute  
 $T \rightarrow int \{T.type = int;\} \Rightarrow$  Synthesized Attribute  
 $\quad /char \{T.type = char;\}$
- $L \rightarrow L_1 id \{L_1.in = L.in, add\ type(id.name, L_1.in);\}$   
 $\quad /id \{add\ type(id.name, L.in) \rightarrow$  Inherited
- L-ATTRIBUTED  
 $int\ x, y, z;$

x	int
y	int
z	int

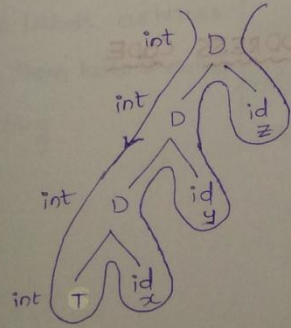


$\Rightarrow$  Evaluate the synthesized attribute when you last visit it

$\Rightarrow$  Evaluate the Inherited attribute when you first visit it.

S-ATTRIBUTED SDT FOR THE SAME QUESTION

- ⑪  $D \rightarrow D_1 id \{add\ type(id.name, D_1.type)\}$   
 $\quad /T id \{add\ type(id.name, T.type), D.type = T.type\}$
- $T \rightarrow int \{T.type = int;\}$   
 $\quad /char \{T.type = char;\}$

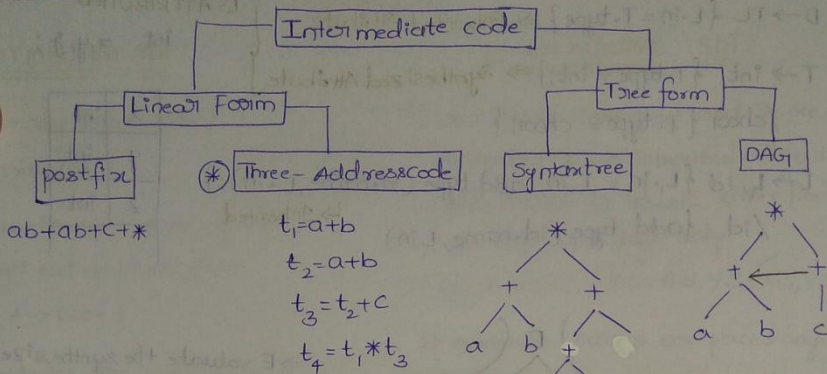


x	int
y	int
z	int

# INTERMEDIATE CODE GENERATION

## INTRODUCTION TO INTERMEDIATE CODE

Ex:  $(a+b)*(a+b+c)$



## TYPES OF 3-ADDRESS CODE

- 1)  $x = y \text{ op } z$  ( $x = a + b$  (Binary operation))
- 2)  $x = \text{op } z$  (Unary operation ( $x = -y$ ))
- 3)  $x = y$  (Assignment)
- 4) if  $x$  (rel op)  $y$  goto L (if 'x' (relational operator)  $y$  goto L)
- 5) goto L  $\Rightarrow$  (unconditional)
- 6)  $A[i] = x$  (Array indexing)  
 $y = A[i]$
- 7)  $x = *p \Rightarrow$  pointer  
 $y = ?y \Rightarrow$  Address of variable assigned to another variable

## VARIOUS REPRESENTATIONS OF 3-ADDRESS CODE

- $\Rightarrow (a+b)*(c+d)+(a+b+c)$
- 1)  $t_1 = a+b$
  - 2)  $t_2 = -t_1$
  - 3)  $t_3 = c+d$
  - 4)  $t_4 = t_2 * t_3$
  - 5)  $t_5 = a+b$
  - 6)  $t_6 = t_5 + c$
  - 7)  $t_7 = t_4 + t_6$

OP
1) +
2) -
3) +
4) *
5) +
6) +
7) +

Adv:  
Arad  
Dis:

## BACK

### Back

if (a < b) else

- (i): if
- (i+1): t
- (i+2): go
- (i+3): t
- (i+4): t

Leaving and f Back

QUADRAPE

Op <sub>r</sub>	Op <sub>1</sub>	Op <sub>2</sub>	Result
1) +	a	b	t <sub>1</sub>
2) -	t <sub>2</sub>	NULL	t <sub>2</sub>
3) +	c	d	t <sub>3</sub>
4) *	t <sub>2</sub>	t <sub>3</sub>	t <sub>4</sub>
5) +	a	b	t <sub>5</sub>
6) +	t <sub>5</sub>	c	t <sub>6</sub>
7) +	t <sub>4</sub>	t <sub>6</sub>	t <sub>7</sub>

Adv: Statements can be moved Around  
Dis: More Space wasted

TRIPLE

Op <sub>r</sub>	Op <sub>1</sub>	Op <sub>2</sub>
1) +	a	b
2) -	(1)	
3) +	c	d
4) *	(3)	(2)
5) +	a	b
6) +	(5)	c
7) +	(4)	(6)

Adv: Space is not wasted  
Dis: Statements cannot be moved

INDIRECT TRIPLE

Op <sub>r</sub>	Op <sub>1</sub>	Op <sub>2</sub>
i) (1)		
ii) (2)		
iii) (3)		
iv) (4)		
v) (5)		
vi) (6)		
vii) (7)		

Adv: State ments can be moved  
Dis: Two Access of Memory.

BACK PATCHING AND CONVERSION TO 3-ADDRESS CODE

Back Patching

```
if (a < b) then t = 1
else t = 0
```

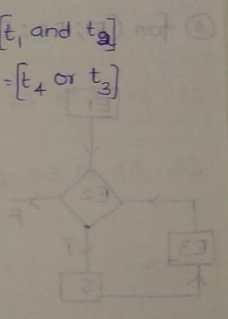
- (i): if a < b goto (i+3)
- (i+1): t = 0
- (i+2): goto (i+4)
- (i+3): t = 1
- (i+4): Return.

Leaving the Labels as blanks and filling them later is called

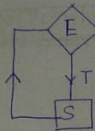
Back patching

```
t1 t2 t3
a < b and c < d or e < f
```

- 100) if (a < b) goto 103      110) goto 112
- 101) t<sub>1</sub> = 0                      111) t<sub>3</sub> = 1
- 102) goto 104
- 103) t<sub>1</sub> = 1
- 104) if (c < d) goto 107
- 105) t<sub>2</sub> = 0
- 106) goto 108
- 107) t<sub>2</sub> = 1
- 108) if (e < f) goto 111
- 109) t<sub>3</sub> = 0



① While E do S



L: if (E==0) goto LI (or) if (E) goto LI  
 S  
 Goto L  
 LI: S  
 goto L

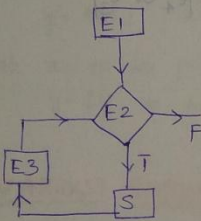
② while (a<b) do  
 x = y + z

L: if a < b goto LI  
 goto last

LI: t = y + z  
 x = t  
 goto L

last:

③ for (E1; E2; E3)



for (i=0; i<10; i++)  
 a = b + c;  
 i = 0

L: if (i < 10) goto LI  
 goto last

LI: t<sub>1</sub> = b + c  
 a = t<sub>1</sub>  
 t = i + 1  
 i = t  
 goto L

last:

④ switch

34

switch

TWO

x = A

t<sub>1</sub> = y

t<sub>2</sub> = t<sub>1</sub>

t<sub>3</sub> = t

t<sub>4</sub> = E

x =

Row M

column

34

```

switch (i+j)
{
  case (i) = a+b+c;
    break;
  case (ii) : p = a+r;
    break;
  default : x = y+z;
    break;
}

```

```

t = i+j
goto test
L1: t1 = b+c
   a = t1
   goto last
L2: t2 = a+r
   p = t2
   goto last
L3: t3 = y+z
   x = t3
   goto last
test: if (t == 1) goto L1
      if (t == 2) goto L2
      goto L3
last:

```

35

### TWO DIMENSIONAL ARRAY TO 3-ADDRESS CODE

$x = A[y][z]$

$$\left. \begin{aligned} t_1 &= y * 20 \\ t_2 &= t_1 + z \\ t_3 &= t_2 * 4 \end{aligned} \right\} (y * 20 + z) * 4$$

$t_4 =$  Base Address of A

$x = t_4[t_3]$

↳ Base offset Addressing  
(Base Address + Offset)

A: 10x20

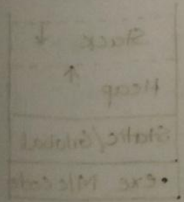
A [4][4]

00	01	02	03
10	11	12	13
20	21	22	23
30	31	32	33

Cross 2' loops  
 ↑  
 A [2][3] columns  
 ↳ No. of elements in row  
 $= 2 * 4 + 3 = 11$

Row Major order: 00 01 02 03 10 11 12 13 20 21 22 23 30 31 32 33

column major order: 00 10 20 30 01 11 21 31 02 12 22 32 03 13 23 33



Activation and deactivation can be in any order  
 ↳ stack: heap management is required  
 ↳ heap: activation can have  
 ↳ permanent lifetime in case of static allocation  
 ↳ limited lifetime in case of stack allocation  
 ↳ dynamic lifetime of heap allocation

# RUN ENVIRONMENT

⇒ Run time Environment means when you run the program what is the support that you need from the operating system.

## STORAGE ALLOCATION STRATEGIES

### 1) Static

- 1) Allocation is done at compile time
- 2) Bindings do not change at Runtime
- 3) One Activation Record per procedure

### Disadvantages

- 1) Recursion is not supported.
- 2) Size of data objects must be known at compile time
- 3) Data structures cannot be created Dynamically

### 2) Stack

whenever a new activation begins, Activation record is pushed onto the Stack and whenever Activation ends, Activation record is popped off

⇒ Local variables are bound to fresh storage

### Disadvantages

- 1) Local variables cannot be retained once activation ends

### 3) Heaps

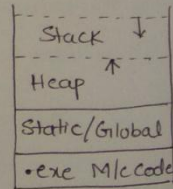
⇒ Allocation and de allocation can be in any order

⇒ Disadv: Heap management is overhead

## SUMMARY

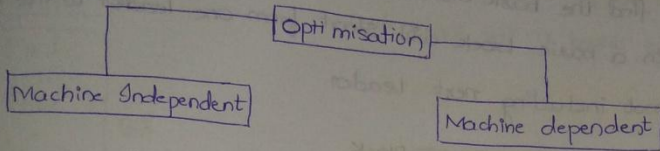
Activations can have

- 1) permanent lifetime in case of static allocation
- 2) Nested lifetime in case of stack Allocation
- 3) Arbitrary lifetime in case of Heap Allocation.



# CODE OPTIMISATION

## INTRODUCTION TO CODE OPTIMISATION



### 1) Loop Optimizations

(a) code motion (const)

frequency reduction

(b) Loop unrolling

(c) Loop Jamming

2) folding

- constant propagation

3) Redundancy Elimination

4) Strength Reduction

1) Register Allocation

2) Use of Addressing modes

3) peephole optimization

(a) Redundant = load/store

(b) Strength Reduction

(c) flow of control options

(d) use of M/C idioms

## LOOP OPTIMISATION AND BASIC BLOCKS

→ To apply optimisations, we must first detect loops

→ For detecting loops we can use control flow Analysis (CFA) using program Flow Graph (PFG)

→ To find PFG, we need to find Basic blocks

A basic block is a sequence of 3-Address statements where control enters at the beginning and leaves at the end without any jumps or halts

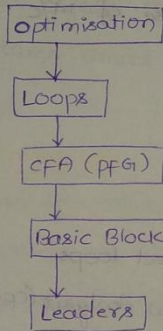
# ALGORITHM TO FIND LEADERS

## Finding the BASIC BLOCKS

→ In order to find the basic blocks, we need to find the leaders in the program then a basic block will start from one leader to the next leader but not including next leader.

## Identifying Leaders in the Basic Block

- 1) I Statement is a leader
- 2) statement that is target of conditional or unconditional statement is a leader → if ( ) goto [200] (or) goto [300] → leader  
↳ Leader
- 3) statement that follows immediately a conditional or unconditional statement is a leader.



## Example

```
fact(x)
{
  int f = 1;
  for(i = 2; i <= x; i++)
  f = f * i;
  return f;
}
```

Now, the

\*1)  $f = 1$

2)  $i = 2$

\*3) if (  $i > x$  )

\*4)  $t_1 = f$

5)  $t_2 = i$

7)  $i = t_2$

8) goto (3)

\*9) Goto (3)

## TYPES

### Frequenc

Moving

frequenc

frequenc

code m

Ex: whi

{

A

i

}

t =

whi

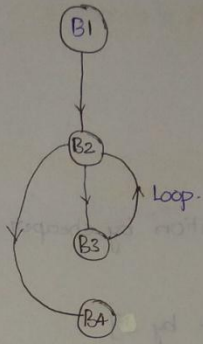
A

Now, the 3-Address code for the above problem will be

```

*1) f = 1      B1
2) i = 2
*3) if (i > x) goto 9 B2
*4) t1 = f * i;
5) t2 = i + 1; B3
7) i = t2;
8) goto (3)
*9) Goto calling program B4
  
```

⇒ In case you have 4 leaders we will get 4 Basic Blocks ⇒ if you have n basic Leaders will get n basic blocks



TYPES OF LOOP OPTIMIZATION

Frequency Reduction

Moving the code from high frequency region to low frequency region is called code motion.

```

Ex: while (i < 5000)
{
  A = sin(x)/cos(x) * i;
  i++;
}
↓
t = sin x / cos x
while (i < 5000)
  A = t * i;
  
```

Loop unrolling

```

while (i < 10)
{
  x[i] = 0;
  i++;
}
↓
while (i < 10)
{
  x[i] = 0;
  i++;
  x[i] = 0;
  i++;
}
  
```

Loop jamming

combines the bodies of two loops

```

for(i=0; i < 10; i++)
  for(j=0; j < 10; j++)
    x[i,j] = 0;
for(i=0; i < 10; i++)
  x[i,i] = 0;
↓
for(i=0; i < 10; i++)
{
  for(j=0; j < 10; j++)
    x[i,j] = 0;
  x[i,i] = 0;
}
  
```

# MACHINE INDEPENDENT OPTIMISATION

## Folding:

Replacing an expression that can be computed at compile time by its value

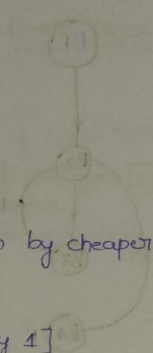
Ex:  $2+3+C+B=5+C+B$

## Redundancy Elimination (DAG)

$$A = B + C$$

$$D = 2 + B + 3 + C$$

$$D = 2 + 3 + A$$



## Strength Reduction

Replacing a costly operation by cheaper one

Ex:  $B = A * 2$

$$B = A \ll 1 \text{ [Left shift by 1]}$$

## Algebraic Simplification

$A = A + 0$   
 $x = x * 1$  } eliminate such statements

# MACHINE DEPENDENT OPTIMISATION

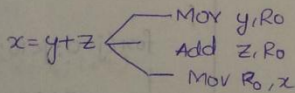
1) Register Allocation 

- Local Allocation
- Global Allocation

2) Use of Addressing modes

3) peephole optimization

a) Redundant Load and store elimination



$a = b + c$  | Mov  $b, R_0$   
 $d = a + e$  | Add  $c, R_0$

Mov $R_0, a$
Mov $a, R_0$

 X  
Add  $e, R_0$   
Mov  $R_0, d$

(b) Flow control optimisation

(91)

Avoid jumps  
on jumps

Eliminate dead  
code

L1: Jump L2<sup>L4</sup>

#define x 0

L2: Jump L3

if (x)

L3: Jump L4

{  
↓ dead code X  
}

d) Use of M/c idioms

i = i + 1	}	Mov R0, i	} increment 'i' [inc i]
		add R0, 1	
		mov i, R0	

⇒ Handle of the string is a substring that matches with RHS of production

⇒ RR conflicts occur in LALR(1) parser when merging of the states

⇒ SR conflicts doesnot occur in LALR(1) parser

⇒ If the attribute can be evaluated in Depth-first-order then the attribute is L-attributed.